

# Package: bliss (via r-universe)

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**Title** Bayesian Functional Linear Regression with Sparse Step Functions

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**Description** A method for the Bayesian functional linear regression model (scalar-on-function), including two estimators of the coefficient function and an estimator of its support. A representation of the posterior distribution is also available. Grollemund P-M., Abraham C., Baragatti M., Pudlo P. (2019) <doi:10.1214/18-BA1095>.

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BIC\_model\_choice      *BIC\_model\_choice*

---

### Description

Model selection with BIC criterion.

### Usage

```
BIC_model_choice(Ks, iter, data, verbose = T)
```

### Arguments

`Ks`                    a numerical vector containing the K values.  
`iter`                    an integer, the number of iteration for each run of `fit_Bliss`.  
`data`                    a list containing required options to run the function `fit_Bliss`.  
`verbose`                write stuff if TRUE (optional).

### Value

A numerical vector, the BIC values for the Bliss model for different K value.

### Examples

```
param_sim <- list(Q=1,n=100,p=c(50),grids_lim=list(c(0,1)))
data        <- sim(param_sim,verbose=TRUE)
iter = 1e2
Ks <- 1:5

res_BIC <- BIC_model_choice(Ks,iter,data)
plot(res_BIC,xlab="K",ylab="BIC")
```

---

`bliss`                    *bliss: Bayesian functional Linear regression with Sparse Step functions*

---

### Description

A method for the Bayesian Functional Linear Regression model (functions-on-scalar), including two estimators of the coefficient function and an estimator of its support. A representation of the posterior distribution is also available.

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**See Also**

Useful links:

- <https://github.com/pmgrollemund/bliss>
- Report bugs at <https://github.com/pmgrollemund/bliss/issues>

---

Bliss\_Gibbs\_Sampler    *Bliss\_Gibbs\_Sampler*

---

**Description**

A Gibbs Sampler algorithm to sample the posterior distribution of the Bliss model.

**Usage**

```
Bliss_Gibbs_Sampler(data, param, verbose = FALSE, to_sample = "posterior")
```

**Arguments**

data	a list containing: <b>y</b> a numerical vector, the outcome values $y_i$ . <b>x</b> a list of matrices, the qth matrix contains the observations of the qth functional covariate at time points given by <b>grids</b> . <b>grids</b> a list of numerical vectors, the qth vector is the grid of time points for the qth functional covariate.
param	a list containing: <b>Q</b> an integer, the number of functional covariates. <b>iter</b> an integer, the number of iterations of the Gibbs sampler algorithm. <b>K</b> a vector of integers, corresponding to the numbers of intervals for each covariate. <b>p</b> an integer, the number of time points. <b>basis</b> a character (optional). The possible values are "uniform" (default), "epanechnikov", "gauss" and "triangular" which correspond to different basis functions to expand the coefficient function and the functional covariates <b>phi_l</b> a numerical (optional). An hyperparameters related to the exponential prior on the length of the intervals. Lower values promotes wider intervals.

**verbose\_cpp** a boolean value (optional). Write stuff from the Rcpp scripts if TRUE.

**verbose** write stuff if TRUE (optional).

**to\_sample** indicates to sample the posterior distribution ("posterior") or the prior distribution ("prior").

### Value

a list containing :

**trace** a matrix, the trace of the Gibbs Sampler.

**param** a list containing parameters used to run the function.

### Examples

```
param_sim <- list(Q=1,n=25,p=50,grids_lim=list(c(0,1)),iter=2e2,K=2)
data_sim <- sim(param_sim,verbose=FALSE)
res_Bliss_Gibbs_Sampler <- Bliss_Gibbs_Sampler(data_sim,param_sim)
theta_1 <- res_Bliss_Gibbs_Sampler$trace[1,]
theta_1
```

---

Bliss\_Simulated\_Annealing

*Bliss\_Simulated\_Annealing*

---

### Description

A Simulated Annealing algorithm to compute the Bliss estimate.

### Usage

```
Bliss_Simulated_Annealing(
  beta_sample,
  posterior_sample,
  param,
  verbose_cpp = FALSE
)
```

### Arguments

**beta\_sample** a matrix. Each row is a coefficient function computed from the posterior sample.

**posterior\_sample** a list resulting from the Bliss\_Gibbs\_Sampler function.

**param** a list containing:

- grids** a list of numerical vectors, the qth vector is the grid of time points for the qth functional covariate.

**basis** a character (optional). The possible values are "uniform" (default), "epanechnikov", "gauss" and "triangular" which correspond to different basis functions to expand the coefficient function and the functional covariates

**burnin** an integer (optional), the number of iteration to drop from the posterior sample.

**iter\_sann** an integer (optional), the number of iteration of the Simulated Annealing algorithm.

**k\_max** an integer (optional), the maximal number of intervals for the Simulated Annealing algorithm.

**l\_max** an integer (optional), the maximal interval length for the Simulated Annealing algorithm.

**Temp\_init** a nonnegative value (optional), the initial temperature for the cooling function of the Simulated Annealing algorithm.

**Q** an integer, the number of functional covariates.

**p** a vector of integers, the numbers of time point of each functional covariate.

**verbose** write stuff if TRUE (optional).

`verbose_cpp` Rcpp writes stuff if TRUE (optional).

## Value

a list containing:

**Bliss\_estimate** a numerical vector, corresponding to the Bliss estimate of the coefficient function.

**Smooth\_estimate** a numerical vector, which is the posterior expectation of the coefficient function for each time points.

**trace** a matrix, the trace of the algorithm.

## Examples

```
data(data1)
data(param1)
data(res_bliss1)
param1$Q <- length(data1$x)
param1$grids <- data1$grids
param1$p <- sapply(data1$grids, length)

posterior_sample <- res_bliss1$posterior_sample
beta_sample <- compute_beta_sample(posterior_sample, param1)

res_sann <- Bliss_Simulated_Annealing(beta_sample, posterior_sample, param1)
```

---

build\_Fourier\_basis     *build\_Fourier\_basis*

---

### Description

Define a Fourier basis to simulate functional covariate observations.

### Usage

```
build_Fourier_basis(grid, dim, per = 2 * pi)
```

### Arguments

grid	a numerical vector.
dim	a numerical value. It corresponds to $\dim(\text{basis})/2$ .
per	a numerical value which corresponds to the period of the sine and cosine functions.

### Details

See the [sim\\_x](#) function.

### Value

a matrix. Each row is an functional observation evaluated on the grid time points.

### Examples

```
# See the function \code{sim_x}.
```

---

change\_grid     *change\_grid*

---

### Description

Compute a function (evaluated on a grid) on a given (finer) grid.

### Usage

```
change_grid(fct, grid, new_grid)
```

### Arguments

fct	a numerical vector, the function to evaluate on the new grid.
grid	a numerical vector, the initial grid.
new_grid	a numerical vector, the new grid.

**Value**

a numerical vector, the approximation of the function on the new grid.

**Examples**

```
grid <- seq(0,1,l=1e1)
new_grid <- seq(0,1,l=1e2)
fct <- 3*grid^2 + sin(grid*2*pi)
plot(grid,fct,type="o",lwd=2,cex=1.5)
lines(new_grid,change_grid(fct,grid,new_grid),type="o",col="red",cex=0.8)
```

---

choose\_beta

*choose\_beta*

---

**Description**

Compute a coefficient function for the Function Linear Regression model.

**Usage**

```
choose_beta(param)
```

**Arguments**

**param** a list containing:

- grid** a numerical vector, the time points.
- p** a numerical value, the length of the vector **grid**.
- shape** a character vector: "smooth", "random\_smooth", "simple", "simple\_bis", "random\_simple", "sinusoid", "flat\_sinusoid" and "sharp"

**Details**

Several shapes are available.

**Value**

A numerical vector which corresponds to the coefficient function at given times points (**grid**).

**Examples**

```
### smooth
param <- list(p=100,grid=seq(0,1,length=100),shape="smooth")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="l")
### random_smooth
param <- list(p=100,grid=seq(0,1,length=100),shape="random_smooth")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="l")
```



```

### simple
param <- list(p=100,grid=seq(0,1,length=100),shape="simple")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="s")
### simple_bis
param <- list(p=100,grid=seq(0,1,length=100),shape="simple_bis")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="s")
### random_simple
param <- list(p=100,grid=seq(0,1,length=100),shape="random_simple")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="s")
### sinusoid
param <- list(p=100,grid=seq(0,1,length=100),shape="sinusoid")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="l")
### flat_sinusoid
param <- list(p=100,grid=seq(0,1,length=100),shape="flat_sinusoid")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="l")
### sharp
param <- list(p=100,grid=seq(0,1,length=100),shape="sharp")
beta_function <- choose_beta(param)
plot(param$grid,beta_function,type="l")

```

---

```

compute_beta_posterior_density
      compute_beta_posterior_density

```

---

## Description

Compute the posterior density of the coefficient function.

## Usage

```
compute_beta_posterior_density(beta_sample, param)
```

## Arguments

<code>beta_sample</code>	a matrix. Each row is a coefficient function computed from the posterior sample.
<code>param</code>	a list containing: <ul style="list-style-type: none"> <li><b>grid</b> a numerical vector, the time points.</li> <li><b>lims_estimate</b> a numerical vector, the time points.</li> <li><b>burnin</b> an integer (optional), the number of iteration to drop from the Gibbs sample.</li> <li><b>lims_kde</b> an integer (optional), correspond to the <code>lims</code> option of the <code>kde2d</code> function.</li> <li><b>new_grid</b> a numerical vector (optional) to compute beta sample on a different grid.</li> <li><b>thin</b> an integer (optional) to thin the posterior sample.</li> </ul>

**Details**

The posterior densities corresponds to approximations of the marginal posterior distributions (of  $\beta(t)$  for each  $t$ ). The sample is thinned in order to reduce the correlation and the computational time of the function [kde2d](#).

**Value**

An approximation of the posterior density on a two-dimensional grid (corresponds to the result of the [kde2d](#) function).

**Examples**

```
library(RColorBrewer)
data(data1)
data(param1)
data(res_bliss1)
param1$grids <- data1$grids
param1$p <- sapply(data1$grids,length)
param1$Q <- length(data1$x)

density_estimate <- compute_beta_posterior_density(res_bliss1$beta_sample,param1)
```

---

compute\_beta\_sample    *compute\_beta\_sample*

---

**Description**

Compute the posterior coefficient function from the posterior sample.

**Usage**

```
compute_beta_sample(posterior_sample, param)
```

**Arguments**

**posterior\_sample** a list provided by the function `Bliss_Gibbs_Sampler`.

**param** a list containing:

- K** a vector of integers, corresponding to the numbers of intervals for each covariate.
- grids** a numerical vector, the observation time points.
- basis** a character (optional) among : "uniform" (default), "epanechnikov", "gauss" and "triangular" which correspond to different basis functions to expand the coefficient function and the functional covariates.
- Q** an integer, the number of functional covariates.
- p** a vector of integers, the numbers of time points of each functional covariate.

**Value**

a matrix containing the coefficient function posterior sample.

**Examples**

```
data(data1)
data(param1)
data(res_bliss1)
param1$grids <- data1$grids
param1$p <- sapply(data1$grids,length)
param1$Q <- length(data1$x)
beta_sample <- compute_beta_sample(posterior_sample=res_bliss1$posterior_sample,
                                   param=param1)
```

---

compute\_chains\_info    *compute\_chains\_info*

---

**Description**

Compute summaries of Gibbs Sampler chains.

**Usage**

```
compute_chains_info(chain, param)
```

**Arguments**

**chain** a list given by the Bliss\_Gibbs\_Sampler function.

**param** a list containing:

- K** a vector of integers, corresponding to the numbers of intervals for each covariate.
- grids** a numerical vector, the observation time points.
- basis** a vector of characters (optional) among : "uniform" (default), "epanechnikov", "gauss" and "triangular" which correspond to different basis functions to expand the coefficient function and the functional covariates.

**Value**

Return a list containing the estimates of mu and sigma\_sq, the Smooth estimate and the chain autocorrelation for mu, sigma\_sq and beta.

**Examples**

```
a=1
```

---

compute\_random\_walk    *compute\_random\_walk*

---

**Description**

Compute a (Gaussian) random walk.

**Usage**

```
compute_random_walk(n, p, mu, sigma, start = rep(0, n))
```

**Arguments**

n	an integer, the number of random walks.
p	an integer, the length of the random walks.
mu	a numerical vector, the mean of the random walks.
sigma	a numerical value which is the standard deviation of the gaussian distribution used to compute the random walks.
start	a numerical vector (optional) which is the initial value of the random walks.

**Details**

See the [sim\\_x](#) function.

**Value**

a matrix where each row is a random walk.

**Examples**

```
# see the sim_x() function.
```

---

compute\_starting\_point\_sann  
                          *compute\_starting\_point\_sann*

---

**Description**

Compute a starting point for the Simulated Annealing algorithm.

**Usage**

```
compute_starting_point_sann(beta_expe)
```

**Arguments**

beta\_expe        a numerical vector, the expectation of the coefficient function posterior sample.

**Value**

a matrix with 3 columns : "m", "l" and "b". The two first columns define the begin and the end of the intervals and the third gives the mean values of each interval.

**Examples**

```
data(res_bliss1)
mystart<-compute_starting_point_sann(apply(res_bliss1$beta_sample[[1]],2,mean))
```

---

corr_matrix	<i>corr_matrix</i>
-------------	--------------------

---

**Description**

Compute an autocorrelation matrix.

**Usage**

```
corr_matrix(diagonal, ksi)
```

**Arguments**

diagonal        a numerical vector corresponding to the diagonal.  
ksi              a numerical value, related to the correlation.

**Value**

a symmetric matrix.

**Examples**

```
### Test 1 : weak autocorrelation
ksi <- 1
diagVar <- abs(rnorm(100,50,5))
Sigma <- corr_matrix(diagVar,ksi^2)
persp(Sigma)
### Test 2 : strong autocorrelation
ksi <- 0.2
diagVar <- abs(rnorm(100,50,5))
Sigma <- corr_matrix(diagVar,ksi^2)
persp(Sigma)
```

---

data1	<i>a list of data</i>
-------	-----------------------

---

**Description**

A data object for bliss model

**Usage**

```
data1
```

**Format**

a list of data

**y** y coordinate

**x** x coordinate

**betas** the coefficient function used to generate the data

**grids** the grid of the observation times

---

determine_intervals	<i>determine_intervals</i>
---------------------	----------------------------

---

**Description**

Determine for which intervals a function is nonnull.

**Usage**

```
determine_intervals(beta_fct)
```

**Arguments**

beta\_fct      a numerical vector.

**Value**

a matrix with 3 columns : "begin", "end" and "value". The two first columns define the begin and the end of the intervals and the third gives the mean values of each interval.

**Examples**

```

data(data1)
data(param1)
# result of res_bliss1<-fit_Bliss(data=data1,param=param1)
data(res_bliss1)
intervals <- determine_intervals(res_bliss1$Bliss_estimate[[1]])
plot(data1$grids[[1]],res_bliss1$Bliss_estimate[[1]],type="s")
for(k in 1:nrow(intervals)){
  segments(data1$grids[[1]][intervals[k,1]],intervals[k,3],
          data1$grids[[1]][intervals[k,2]],intervals[k,3],col=2,lwd=4)
}

```

---

do\_need\_to\_reduce      *do\_need\_to\_reduce*

---

**Description**

Determine if it is required to reduce the size of the grid time points for each functional covariate.

**Usage**

```
do_need_to_reduce(param)
```

**Arguments**

param            a list containing `p_threshold` the maximum number of time points and `p` the actual number of time points for each functional covariate.

**Value**

a boolean value.

**Examples**

```

data(param1)
param1$p <- sapply(data1$grids,length)

do_need_to_reduce(param1)

```

---

`dposterior`*dposterior*

---

### Description

Compute (non-normalized) posterior densities for a given parameter set.

### Usage

```
dposterior(posterior_sample, data, theta = NULL)
```

### Arguments

`posterior_sample` a list given by the `Bliss_Gibbs_Sampler` function.

`data` a list containing

- `y` a numerical vector, the outcomes.
- `x` a list of matrices, the `q`th matrix contains the observations of the `q`th functional covariate at time points given by `grids`.

`theta` a matrix or a vector which contains the parameter set.

### Details

If the `theta` is `NULL`, the posterior density is computed from the MCMC sample given in the `posterior_sample`.

### Value

Return the (log) posterior density, the (log) likelihood and the (log) prior density for the given parameter set.

### Examples

```
data(data1)
data(param1)
# result of res_bliss1<-fit_Bliss(data=data1,param=param1)
data(res_bliss1)
# Compute the posterior density of the MCMC sample :
res_poste <- dposterior(res_bliss1$posterior_sample,data1)
```



---

fit_Bliss	<i>fit_Bliss</i>
-----------	------------------

---

## Description

Fit the Bayesian Functional Linear Regression model (with Q functional covariates).

## Usage

```
fit_Bliss(
  data,
  param,
  sann = TRUE,
  compute_density = TRUE,
  support_estimate = TRUE,
  sann_trace = FALSE,
  verbose = TRUE
)
```

## Arguments

data	<p>a list containing:</p> <ul style="list-style-type: none"> <li><b>y</b> a numerical vector, the outcomes.</li> <li><b>x</b> a list of matrices, the qth matrix contains the observations of the qth functional covariate at time points given by <b>grids</b>.</li> <li><b>grids</b> a list of numerical vectors, the qth vector is the grid of time points for the qth functional covariate.</li> </ul>
param	<p>a list containing:</p> <ul style="list-style-type: none"> <li><b>iter</b> an integer, the number of iterations of the Gibbs sampler algorithm.</li> <li><b>K</b> a vector of integers, corresponding to the numbers of intervals for each covariate.</li> <li><b>basis</b> a character vector (optional). The possible values are "uniform" (default), "epanechnikov", "gauss" and "triangular" which correspond to different basis functions to expand the coefficient function and the functional covariates</li> <li><b>burnin</b> an integer (optional), the number of iteration to drop from the posterior sample.</li> <li><b>iter_sann</b> an integer (optional), the number of iteration of the Simulated Annealing algorithm.</li> <li><b>k_max</b> an integer (optional), the maximal number of intervals for the Simulated Annealing algorithm.</li> <li><b>l_max</b> an integer (optional), the maximal interval length for the Simulated Annealing algorithm.</li> <li><b>lims_kde</b> an integer (optional), correspond to the <b>lims</b> option of the <b>kde2d</b> function.</li> </ul>

	<b>new_grids</b> a list of Q vectors (optional) to compute beta samples on different grids.
	<b>Temp_init</b> a nonnegative value (optional), the initial temperature for the cooling function of the Simulated Annealing algorithm.
	<b>thin</b> an integer (optional) to thin the posterior sample.
	<b>times_sann</b> an integer (optional), the number of times the algorithm will be executed
	<b>times_sann</b> an integer (optional), the number of times the algorithm will be executed
	<b>allow_reducing</b> a boolean value (optional), indicate if the function is allowed to reduce the number of sample times of each functional covariate.
	<b>verbose_cpp</b> a boolean value (optional). Write stuff from the Rcpp scripts if TRUE.
sann	a logical value. If TRUE, the Bliss estimate is computed with a Simulated Annealing Algorithm. (optional)
compute_density	a logical value. If TRUE, the posterior density of the coefficient function is computed. (optional)
support_estimate	a logical value. If TRUE, the estimate of the coefficient function support is computed. (optional)
sann_trace	a logical value. If TRUE, the trace of the Simulated Annealing algorithm is included into the result object. (optional)
verbose	write stuff if TRUE (optional).

## Value

return a list containing:

- alpha** a list of Q numerical vector. Each vector is the function  $\alpha(t)$  associated to a functional covariate. For each t,  $\alpha(t)$  is the posterior probabilities of the event "the support covers t".
- beta\_posterior\_density** a list of Q items. Each item contains a list containing information to plot the posterior density of the coefficient function with the image function.
  - grid\_t a numerical vector: the x-axis.
  - grid\_beta\_t a numerical vector: the y-axis.
  - density a matrix: the z values.
  - new\_beta\_sample a matrix: beta sample used to compute the posterior densities.
- beta\_sample** a list of Q matrices. The qth matrix is a posterior sample of the qth functional covariates.
- Bliss\_estimate** a list of numerical vectors corresponding to the Bliss estimates of each functional covariates.
- data** a list containing the data.
- posterior\_sample** a list of information about the posterior sample: the trace matrix of the Gibbs sampler, a list of Gibbs sampler parameters and the posterior densities.

**support\_estimate** a list of support estimates of each functional covariate.

**support\_estimate\_fct** another version of the support estimates.

**trace\_sann** a list of Q matrices which are the trace of the Simulated Annealing algorithm.

### Examples

```
# see the vignette BlissIntro.
```

---

<code>image_Bliss</code>	<i>image_Bliss</i>
--------------------------	--------------------

---

### Description

Plot an approximation of the posterior density.

### Usage

```
image_Bliss(beta_posterior_density, param = list(), q = 1, to_print = TRUE)
```

### Arguments

<code>beta_posterior_density</code>	a list. The result of the function <code>compute_beta_posterior_density</code> .
<code>param</code>	an optional list containing arguments: <code>col_low</code> , <code>col_mid</code> , <code>col_high</code> , <code>ylim</code> , <code>xlab</code> , <code>ylab</code> , <code>title</code> .
<code>q</code>	an integer (optional), the index of the functional covariate to plot.
<code>to_print</code>	display the plot if TRUE.

### Examples

```
data(data1)
data(param1)
data(res_bliss1)

image_Bliss(res_bliss1$beta_posterior_density,param1,q=1)
```

---

integrate\_trapeze      *integrate\_trapeze*

---

**Description**

Trapezoidal rule to approximate an integral.

**Usage**

```
integrate_trapeze(x, y)
```

**Arguments**

`x`                    a numerical vector, the discretization of the domain.  
`y`                    a numerical value, the discretization of the function to integrate.

**Value**

a numerical value, the approximation.

**Examples**

```
x <- seq(0,1,le=1e2)
integrate_trapeze(x,x^2)

integrate_trapeze(data1$grids[[1]],t(data1$x[[1]]))
```

---

interpretation\_plot      *interpretation\_plot*

---

**Description**

Provide a graphical representation of the functional data with a focus on the detected periods with the Bliss method.

**Usage**

```
interpretation_plot(data, Bliss_estimate, q = 1, centered = FALSE, cols = NULL)
```

**Arguments**

<code>data</code>	a list containing:  <b>y</b> a numerical vector, the outcomes. <b>x</b> a list of matrices, the qth matrix contains the observations of the qth functional covariate at time points given by <code>grids</code> . <b>grids</b> a list of numerical vectors, the qth vector is the grid of time points for the qth functional covariate.
<code>Bliss_estimate</code>	a numerical vector, the Bliss estimate.
<code>q</code>	an integer (optional), the index of the functional covariate to plot.
<code>centered</code>	a logical value (optional), If TRUE, the functional data are centered.
<code>cols</code>	a numerical vector of colours (optional).

**Examples**

```

data(data1)
data(param1)
# result of res_bliss1 <- fit_Bliss(data=data1,param=param1,verbose=TRUE)
data(res_bliss1)
interpretation_plot(data=data1,Bliss_estimate=res_bliss1$Bliss_estimate,q=1)
interpretation_plot(data=data1,Bliss_estimate=res_bliss1$Bliss_estimate,q=1,centered=TRUE)

```

---

lines\_bliss

*lines\_bliss*

---

**Description**

Add a line to a plot obtained with `image_Bliss`.

**Usage**

```
lines_bliss(x, y, col = "black", lty = "solid")
```

**Arguments**

<code>x</code>	the coordinates of points in the plot.
<code>y</code>	the y coordinates of points in the plot.
<code>col</code>	a color.
<code>lty</code>	option corresponding to "linetype" of <code>geom_line</code> .

**Examples**

```

data(data1)
data(param1)
data(res_bliss1)

image_Bliss(res_bliss1$beta_posterior_density,param1,q=1) +
lines_bliss(res_bliss1$data$grids[[1]],res_bliss1$smooth_estimate[[1]])+
lines_bliss(res_bliss1$data$grids[[1]],res_bliss1$Bliss_estimate[[1]],col="purple")

```

---

param1	<i>A list of param for bliss model</i>
--------	--

---

**Description**

A list of param for bliss model

**Usage**

```
param1
```

**Format**

a list of param for bliss model

**Q** the number of functional covariates

**n** the sample size

**p** the number of observation times

**beta\_shapes** the shapes of the coefficient functions

**grids\_lim** the range of the observation times

**grids** the grids of the observation times

**K** the number of intervals for the coefficient function

---

pdexp	<i>pdexp</i>
-------	--------------

---

**Description**

Probability function of a discretized Exponential distribution.

**Usage**

```
pdexp(a, l_values)
```

**Arguments**

`a` a positive value, the mean of the Exponential prior.  
`l_values` a numerical value, the discrete support of the parameter  $\lambda$ .

**Value**

a numerical vector, which is the probability function on `l_values`.

**Examples**

```
pdexp(10, seq(0, 1, 1))

x <- seq(0, 10, le=1e3)
plot(x, dexp(x, 0.5), lty=2, type="l")
lines(pdexp(0.5, 1:10), type="p")
```

---

post\_treatment\_bliss *post\_treatment\_bliss*

---

**Description**

Compute the post treatment values.

**Usage**

```
post_treatment_bliss(posterior_sample, param, data)
```

**Arguments**

`posterior_sample`  
a list provided by the function `Bliss_Gibbs_Sampler`.  
`param`  
a list containing:  
**K** a vector of integers, corresponding to the numbers of intervals for each covariate.  
`data`  
a list containing required options to run the function `dposterior`.

**Value**

A list of important post treatment value: BIC, the maximum of the log likelihood and the number of parameters.

**Examples**

```
data(data1)
data(param1)
data(res_bliss1)

post_treatment_bliss(res_bliss1$posterior_sample, param1, data1)
```

---

predict\_bliss      *predict\_bliss*

---

**Description**

Compute predictions.

**Usage**

```
predict_bliss(x, grids, burnin, posterior_sample, Smooth_estimate)
```

**Arguments**

**x**                    a list containing the design matrices related to the functional covariates. Must be similar to the result of the function `sim_x`.

**grids**                a list of numerical vectors, the *q*th vector is the grid of time points for the *q*th functional covariate.

**burnin**                an integer (optional), the number of iteration to drop from the posterior sample.

**posterior\_sample**    a list provided by the function `Bliss_Gibbs_Sampler`.

**Smooth\_estimate**    one of the objects resulting from `Bliss_Simulated_Annealing`.

**Value**

A vector of predictions for each individual data *x*.

**Examples**

```
data(data1)
data(param1)
data(res_bliss1)

predict_bliss(data1$x, data1$grids, 50, res_bliss1$posterior_sample, res_bliss1$smooth_estimate)
```

---

predict\_bliss\_distribution  
*predict\_bliss\_distribution*

---

**Description**

Compute the distribution of the predictions.



**Usage**

```
predict_bliss_distribution(x, grids, burnin, posterior_sample, beta_sample)
```

**Arguments**

`x` a list containing the design matrices related to the functional covariates. Must be similar to the result of the function `sim_x`.

`grids` a list of numerical vectors, the `q`th vector is the grid of time points for the `q`th functional covariate.

`burnin` an integer (optional), the number of iteration to drop from the posterior sample.

`posterior_sample` a list provided by the function `Bliss_Gibbs_Sampler`.

`beta_sample` a list provided by the function `compute_beta_sample`.

**Value**

A matrix containing predictions for each individual data `x`.

**Examples**

```
data(data1)
data(param1)
data(res_bliss1)

predict_bliss_distribution(data1$x, data1$grids, 50, res_bliss1$posterior_sample,
  res_bliss1$beta_sample)
```

---

```
printbliss          Print a bliss Object
```

---

**Description**

Print a bliss Object

**Usage**

```
printbliss(x, ...)
```

**Arguments**

`x` input bliss Object

`...` further arguments passed to or from other methods

**Examples**

```
# See fit_Bliss() function
```

---

reduce_x	<i>reduce_x</i>
----------	-----------------

---

**Description**

Reduce the number of time points.

**Usage**

```
reduce_x(data, param)
```

**Arguments**

data	similar to fit_Bliss.
param	a list containing values Q, p and p

**Value**

a numerical value, the approximation.

**Examples**

```
param <- list(Q=1, n=10, p=c(150), grids_lim=list(c(0,1)))
data <- sim(param)

data(param1)
param1$n <- nrow(data$x[[1]])
param1$p <- sapply(data$grids, length)
param1$Q <- length(data$x)

data <- reduce_x(data, param1)
```

---

res_bliss1	<i>A result of the BliSS method</i>
------------	-------------------------------------

---

**Description**

A result of the BliSS method

**Usage**

```
res_bliss1
```

**Format**

a Bliss object (list)

**alpha** a list of Q numerical vector. Each vector is the function  $\alpha(t)$  associated to a functional covariate. For each t,  $\alpha(t)$  is the posterior probabilities of the event "the support covers t".

**beta\_posterior\_density** a list of Q items. Each item contains a list containing information to plot the posterior density of the coefficient function with the image function.

**grid\_t** a numerical vector: the x-axis.

**grid\_beta\_t** a numerical vector: the y-axis.

**density** a matrix: the z values.

**new\_beta\_sample** a matrix: beta sample used to compute the posterior densities.

**beta\_sample** a list of Q matrices. The qth matrix is a posterior sample of the qth functional covariates.

**Bliss\_estimate** a list of numerical vectors corresponding to the Bliss estimates of each functional covariates.

**data** see the description of the object `data1`.

**posterior\_sample** a list containing (for each chain) the result of the `Bliss_Gibbs_Sampler` function.

**Smooth\_estimate** a list containing the Smooth estimates of the coefficient functions.

**support\_estimate** a list containing the estimations of the support.

**support\_estimate\_fct** a list containing the estimation of the support.

**trace\_sann** a list containing (for each chain) the trace of the Simulated Annealing algorithm.

---

sigmoid

*sigmoid*

---

**Description**

Compute a sigmoid function.

**Usage**

```
sigmoid(x, asym = 1, v = 1)
```

**Arguments**

**x** a numerical vector, time points.

**asym** a numerical value (optional), the asymptote of the sigmoid function.

**v** a numerical value (optional), related to the slope at the origin.

**Details**

see the function [sim\\_x](#).

**Value**

a numerical vector.

**Examples**

```
## Test 1 :
x <- seq(-7,7,0.1)
y <- sigmoid(x)
plot(x,y,type="l",main="Sigmoid function")
## Test 2 :
x <- seq(-7,7,0.1)
y <- sigmoid(x)
y2 <- sigmoid(x,asym=0.5)
y3 <- sigmoid(x,v = 5)
plot(x,y,type="l",main="Other sigmoid functions")
lines(x,y2,col=2)
lines(x,y3,col=3)
```

---

sigmoid\_sharp

*sigmoid\_sharp*

---

**Description**

Compute a sharp sigmoid function.

**Usage**

```
sigmoid_sharp(x, loc = 0, ...)
```

**Arguments**

x	a numerical vector, time points.
loc	a numerical value (optional), the time of the sharp.
...	Arguments (optional) for the function sigmoid.

**Details**

see the function [sim\\_x](#).

**Value**

a numerical vector.

## Examples

```
## Test 1 :
x <- seq(-7,7,0.1)
y <- sigmoid_sharp(x)
plot(x,y,type="l",main="Sharp sigmoid")
## Test 2 :
x <- seq(-7,7,0.1)
y <- sigmoid_sharp(x,loc=3)
y2 <- sigmoid_sharp(x,loc=3,asym=0.5)
y3 <- sigmoid_sharp(x,loc=3,v = 5)
plot(x,y,type="l",main="Other sharp sigmoids")
lines(x,y2,col=2)
lines(x,y3,col=3)
```

---

sim

*sim*

---

## Description

Simulate a dataset for the Function Linear Regression model.

## Usage

```
sim(param, verbose = FALSE)
```

## Arguments

**param** a list containing:

- beta\_shapes** a character vector. The qth item indicates the shape of the coefficient function associated to the qth functional covariate.
- beta\_functions** a list containing numerical vectors to define the beta functions
- n** an integer, the sample size.
- p** a vector of integers, the qth component is the number of times for the qth covariate.
- Q** an integer, the number of functional covariates.
- autocorr\_diag** a list of numerical vectors (optional), the qth vector is the diagonal of the autocorrelation matrix of the qth functional covariate.
- autocorr\_spread** a vector of numerical values (optional) which are related to the autocorrelation of the functional covariates.
- grids** a list of numerical vectors (optional), the qth vector is the grid of time points for the qth functional covariate.
- grids\_lim** a list of numerical vectors (optional), the qth item is the lower and upper boundaries of the domain for the qth functional covariate.
- link** a function (optional) to simulate data from the Generalized Functional Linear Regression model.
- mu** a numerical value (optional), the 'true' intercept of the model.

**r** a nonnegative value (optional), the signal to noise ratio.

**x\_shapes** a character vector (optional). The qth item indicates the shape of the functional covariate observations.

verbose write stuff if TRUE.

### Value

a list containing:

**Q** an integer, the number of functional covariates.

**y** a numerical vector, the outcome observations.

**x** a list of matrices, the qth matrix contains the observations of the qth functional covariate at time points given by grids.

**grids** a list of numerical vectors, the qth vector is the grid of time points for the qth functional covariate.

**betas** a list of numerical vectors, the qth vector is the 'true' coefficient function associated to the qth covariate on a grid of time points given with grids.

### Examples

```
library(RColorBrewer)
param <- list(Q=2, n=25, p=c(50, 50), grids_lim=list(c(0, 1), c(-1, 2)))
data <- sim(param)
data$y
cols <- colorRampPalette(brewer.pal(9, "Yl0rRd"))(10)
q=2
matplot(data$grids[[q]], t(data$x[[q]]), type="l", lty=1, col=cols)
plot(data$grids[[q]], data$betas[[q]], type="l")
abline(h=0, lty=2, col="gray")
```

---

sim\_x

sim\_x

---

### Description

Simulate functional covariate observations.

### Usage

```
sim_x(param)
```

**Arguments**

**param** a list containing :

- grid** a numerical vector, the observation times.
- n** an integer, the sample size.
- p** an integer, the number of observation times.
- diagVar** a numerical vector (optional), the diagonal of the autocorrelation matrix.
- dim** a numerical value (optional), the dimension of the Fourier basis, if "shape" is "Fourier" or "Fourier2".
- ksi** a numerical value (optional) related to the observations correlation.
- x\_shape** a character vector (optional), the shape of the observations.

**Details**

Several shape are available for the observations: "Fourier", "Fourier2", "random\_walk", "random\_sharp", "uniform", "gaussian", "mvgauss", "mvgauss\_different\_scale", "mvgauss\_different\_scale2", "mvgauss\_different\_scale3" and "mvgauss\_different\_scale4".

**Value**

a matrix which contains the functional covariate observations at time points given by grid.

**Examples**

```
library(RColorBrewer)
### uniform
param <- list(n=15,p=100,grid=seq(0,1,length=100),x_type="uniform")
x <- sim_x(param)
cols <- colorRampPalette(brewer.pal(9,"Yl0rRd"))(15)
matplot(param$grid,t(x),type="l",lty=1,col=cols)
```

---

support\_estimation      *support\_estimation*

---

**Description**

Compute the support estimate.

**Usage**

```
support_estimation(beta_sample, param)
```

**Arguments**

**beta\_sample** the result of the function compute\_beta\_sample.

**param** a list containing the value Q and an optional parameter gamma.

**Value**

a list containing:

**alpha** a numerical vector. The approximated posterior probabilities that the coefficient function support covers  $t$  for each time points  $t$ .

**estimate** a numerical vector, the support estimate.

**estimate\_fct** a numerical vector, another version of the support estimate.

**Examples**

```
data(data1)
data(param1)
data(res_bliss1)
param1$Q <- length(data1$x)

res_support <- support_estimation(res_bliss1$beta_sample,param1)
```

---

<i>%between%</i>	<i>between</i>
------------------	----------------

---

**Description**

Check if a number belong to a given interval.

**Usage**

```
value %between% interval
```

**Arguments**

**value** a numerical value.

**interval** a numerical vector: (lower,upper).

**Value**

a logical value.

**Examples**

```
1 %between% c(0,2)
2 %between% c(0,2)
3 %between% c(0,2)
```



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